Synthesis

CS294-184: Building User-Centered Programming Tools

UC Berkeley Sarah E. Chasins

Program Synthesis Week 2, Day 1



Discuss in groups

- How would the different synthesis approaches described in the reading affect the user interaction model?
- How would the approaches described in the reading apply or not apply to the various synthesis project ideas you brainstormed last Tuesday?
- Please also take a couple minutes to discuss what you learned from the Rosette assignment!

Reading Reflection

Reading Key Takeaways



Figure 3.2: Counterexample-guided inductive synthesis.

- programs produce different outputs.
 - project! See Fig 3.10 for how nice the programs are.



• Distinguishing inputs—2 programs match our spec. How will we find the one we want? Ask the user what we should do on this next input, for which the

Syntactic bias—as we've already discussed, language shapes the search space • SyGuS—SyGuS solvers can be a really useful starting point for a new synthesis

SyGuS string example

(set-logic SLIA)

(synth-fun f ((name String)) String ((Start String (ntString)) (ntString String (name " " "." "Dr." (str.++ ntString ntString) (str.substr ntString ntInt ntInt))) (ntInt Int (0 1 2 (+ ntInt ntInt) (- ntInt ntInt) (str.len ntString) (str.to.int ntString) (str.indexof ntString ntString ntInt))) (ntBool Bool (true false (str.prefixof ntString ntString) (str.suffixof ntString ntString) (str.contains ntString ntString))))

```
(declare-var name String)
(constraint (= (f "Nancy FreeHafer") "Dr. Nancy"))
(constraint (= (f "Andrew Cencici") "Dr. Andrew"))
(constraint (= (f "Jan Kotas") "Dr. Jan"))
(constraint (= (f "Mariya Sergienko") "Dr. Mariya"))
```

(check-synth)

```
(str.replace ntString ntString ntString) (str.at ntString ntInt) (int.to.str ntInt)
```

What did you learn from the Rosette activity (or HW)?

A few learning goals

You might have learned...

- That you can write a synthesizer!
- That there are many possible ways of designing the grammar, many possible ways of designing the spec A visceral understanding of the difference between finding a program that meets your spec and the program you actually want. :) Especially in example-based specs.
- The limits of what you can control in Rosette.



Armando Solar-Lezama

One (of many) solutions

```
(define-synthax (is-title x depth)
#:base (choose #t #f)
#:else (choose
        #t #f
         (if ((choose < >) ((choose get-font-size get-num-words) x) (??))
             (is-title x (- depth 1))
             (is-title x (- depth 1))))
(define (is-title-synthesized x)
 (is-title x 1))
(define-symbolic i integer?)
(print-forms
 (synthesize
 #:forall (list i)
 #:guarantee (assert (or
                       (< i 0)
                       (>= i (length texts))
```

```
Welcome to DrRacket, version 7.8 [3m].
Language: rosette/safe, with debugging; memory limit: 256 MB.
20
450
#f
/Users/schasins/Documents/titleDetection.rkt:49:0
'(define (is-title-synthesized x) (if (> (get-font-size x) 31) #t #f))
>
```

(equal? (is-title-synthesized (list-ref texts i)) (get-is-title (list-ref texts i))))))

```
(define texts
 [list (list 20 450 #f) (list 30 1200 #f) (list 70 4 #t) (list 72 9 #t) (list 9 4 #f) (list 72 200 #f)])
(define (get-font-size t)
 (list-ref t 0))
                                                                                                     get more complicated
(define (get-num-words t)
 (list-ref t 1))
(define (get-is-title t)
                                                                                                     inputs from our user...
 (list-ref t 2))
(get-font-size (list-ref texts 0))
(get-num-words (list-ref texts 0))
(get-is-title (list-ref texts 0))
                                                                                                   Original input-output pairs
; Now write a synthesizer that can learn a program for labeling texts as titles
; or not titles based on the examples in our texts list.
; Hint: if you end up using the #:forall (list i) approach in your solution,
; remember that i can be less than 0 and greater than the length of the texts
; list.
                                                                                                   Here we add 3 more
; Defines a grammar
(define-synthax (is-title x depth)
#:base (choose #t #f)
#:else (choose
       #t #f
       (if ((choose < >) ((choose get-font-size get-num-words) x) (??))
           (is-title x (- depth 1))
                                                                                                                                                 quote
           (is-title x (- depth 1))))
(define (is-title-synthesized x)
 (is-title x 2))
                                                                                                 The same synthesizer now produces:
(define-symbolic i integer?)
(print-forms
                                                                                     '(define (is-title-synthesized x)
 (synthesize
                                                                                        (if (< (get-font-size x) 69) #f (if (< (get-num-words x) 200) #t #f)))</pre>
 #:forall (list i)
 #: guarantee (assert (or
                    (< i 0)
                    (>= i (length texts))
                    (equal? (is-title-synthesized (list-ref texts i)) (get-is-title (list-ref texts i))))))
```

```
Welcome to DrRacket, version 7.8 [3m].
Language: rosette/safe, with debugging; memory limit: 256 MB.
20
450
#f
/Users/schasins/Documents/titleDetection.rkt:49:0
'(define (is-title-synthesized x)
   (if (< (get-font-size x) 69) #f (if (< (get-num-words x) 200) #t #f)))
```

And this is adaptable as we

(list 20 450 #f) (list 30 1200 #f) (list 70 4 #t) (list 72 9 #t) (list 9 4 #f) (list 72 200 #f)]) mavbe a footnote maybe a pull-out



```
(define (hole depth arity non-terms terms)
  ...) ; Expression hole (Section 2.2)
(define (F<sub>Alglave</sub> ppo grf fences)
  ...) ; Axioms from Figure 4
(define rfi (& rf (join thd (~ thd))))
(define rfe (- rf (join thd (~ thd))))
 Expression holes for F_{Alglave} model (Section 3.2)
(define ppo
  (hole 4 2 (list + - -> \& SameAddr)
            (list po dep Event Read Write Fence Atomic)))
(define grf (hole 4 2 (list + - -> & SameAddr)
                       (list rf rfi rfe none univ)))
; x86 fences are not cumulative
(define fences (-> none none))
; Final sketch
(define x86-sketch (F<sub>Alglave</sub> ppo grf fences))
```

(a) Framework sketch *F*_{Alglave}

(b) Synthesized models TSO_0 and TSO_4

Figure 9. The framework sketch $F_{Alglave}$ for synthesizing a memory model for the x86 architecture (a), and synthesized models TSO_0 and TSO_4 before and after resolving ambiguities (b). The expression holes for ppo and grf define a search space of size 2^{624} , as described in Figure 8. The fences relation is empty because x86 fences are not cumulative.



; Common components of memory model specifications (define (SameAddr X) (& (-> X X) (join loc (~ loc)))) Rosette for more realistic tasks...



Synthesizing Memory Models from Framework Sketches and Litmus Tests

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Abstract

A memory consistency model specifies which writes to shared memory a given read may see. Ambiguities or errors in these specifications can lead to bugs in both compilers and applications. Yet architectures usually define their memory models with prose and *litmus tests*—small concurrent programs that demonstrate allowed and forbidden outcomes. Recent work has formalized the memory models of common architectures through substantial manual effort, but as new architectures emerge, there is a growing need for tools to aid these efforts.

This paper presents MemSynth, a synthesis-aided system for reasoning about axiomatic specifications of memory models. MemSynth takes as input a set of litmus tests and a *framework sketch* that defines a class of memory models. The sketch comprises a set of axioms with missing expressions (or *holes*). Given these inputs, MemSynth synthesizes a completion of the axioms—i.e., a memory model—that gives the desired outcome on all tests. The MemSynth engine

1. Introduction

Reasoning about concurrent code requires a *memory consistency model* that specifies the memory reordering behaviors the hardware will expose. Architectures typically define their memory consistency model with prose and *litmus tests*, small programs that illustrate allowed and forbidden outcomes. These imprecise definitions make reasoning about correctness difficult for both developers and tool builders. Researchers have therefore argued for formalizing memory models [49], and have recently created formal models for common architectures, including x86 [40] and PowerPC [30]. But each such formalization required several person-years of effort and several revisions (e.g., [5, 6, 35, 38, 39]).

These formalization efforts have been aided by tools for *verification* and *comparison* of memory models. Verification tools check whether a model allows a litmus test [6, 36, 45], while comparison tools synthesize litmus tests on which two models disagree [28, 47]. These tools provide verification and

```
#lang rosette
     ; import serval core functions with prefix "serval:"
    (require (prefix-in serval: serval/lib/core))
    ; cpu state: program counter and integer registers
    (struct cpu (pc regs) #:mutable)
    ; interpret a program from a given cpu state
    (define (interpret c program)
10
       (serval:split-pc [cpu pc] c
11
12
         ; fetch an instruction to execute
13
         (define insn (fetch c program))
         ; decode an instruction into (opcode, rd, rs, imm)
14
15
         (match insn
          [(list opcode rd rs imm)
16
17
             ; execute the instruction
18
             (execute c opcode rd rs imm)
             ; recursively interpret a program until "ret"
19
20
            (when (not (equal? opcode 'ret))
21
              (interpret c program))])))
22
23
     ; fetch an instruction based on the current pc
^{24}
    (define (fetch c program)
      (define pc (cpu-pc c))
25
       ; the behavior is undefined if pc is out-of-bounds
26
27
       (serval:bug-on (< pc 0))
28
      (serval:bug-on (>= pc (vector-length program)))
29
       : return the instruction at program[pc]
30
      (vector-ref program pc))
31
     ; shortcut for getting the value of register rs
32
    (define (cpu-reg c rs)
33
34
      (vector-ref (cpu-regs c) rs))
35
36
     ; shortcut for setting register rd to value v
37
    (define (set-cpu-reg! c rd v)
38
      (vector-set! (cpu-regs c) rd v))
39
40
    ; execute one instruction
    (define (execute c opcode rd rs imm)
41
      (define pc (cpu-pc c))
42
43
      (case opcode
        [(ret) ; return
44
45
          (set-cpu-pc! c 0)]
46
        [(bnez) ; branch to imm if rs is nonzero
47
48
          (if (! (= (cpu-reg c rs) 0))
               (set-cpu-pc! c imm)
49
               (set-cpu-pc! c (+ 1 pc)))]
50
51
        [(sgtz) ; set rd to 1 if rs > 0, 0 otherwise
          (set-cpu-pc! c (+ 1 pc))
52
          (if (> (cpu-reg c rs) 0)
53
               (set-cpu-reg! c rd 1)
54
               (set-cpu-reg! c rd 0))]
55
56
        [(sltz) ; set rd to 1 if rs < 0, 0 otherwise
           (set-cpu-pc! c (+ 1 pc))
57
           (if (< (cpu-reg c rs) 0)
58
59
               (set-cpu-reg! c rd 1)
               (set-cpu-reg! c rd 0))]
60
         [(li) ; load imm into rd
61
          (set-cpu-pc! c (+ 1 pc))
62
          (set-cpu-reg! c rd imm)]))
```

Figure 4. A ToyRISC interpreter using Serval (in Rosette).

This paper presents Serval, a framework for developing automated verifiers for systems software. Serval provides an extensible infrastructure for creating verifiers by lifting interpreters under symbolic evaluation, and a systematic approach to identifying and repairing verification performance bottlenecks using symbolic profiling and optimizations. Using Serval, we build automated verifiers for the RISC-V,

x86-32, LLVM, and BPF instruction sets. We report our experience of retrofitting CertiKOS and Komodo, two systems previously verified using Coq and Dafny, respectively, for automated verification using Serval, and discuss trade-offs of different verification methodologies. In addition, we apply Serval to the Keystone security monitor and the BPF compilers in the Linux kernel, and uncover 18 new bugs through verification, all confirmed and fixed by developers.

ACM Reference Format: Luke Nelson, James Bornholt, Ronghui Gu, Andrew Baumann, Emina Torlak, and Xi Wang, 2019. Scaling symbolic evaluation for

Rosette for more realistic tasks...



Scaling symbolic evaluation for automated verification of systems code with Serval

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Ronghui Gu Columbia University

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Abstract

But the benefits of formal verification come at a considerable cost. Writing proofs requires a time investment that is usually measured in person-years, and the size of proofs can be several times or even more than an order of magnitude larger than that of implementation code [49: §7.2].

The push-button verification approach [65, 74, 75] frees developers from such proof burden through co-design of systems and verifiers to achieve a high degree of automation, at the cost of generality. This approach asks developers to design interfaces to be finite so that the semantics of each interface operation (such as a system call) is expressible as a set of traces of bounded length (i.e., the operation can be implemented without using unbounded loops). Given the problem of verifying a finite implementation against its specification, a domain-specific automated verifier reduces this problem to a satisfiability query using symbolic evaluation [32] and discharges the query with a solver such as Z3 [31].

While promising, this co-design approach raises three open questions: How can we write automated verifiers that

Reflections on Rosette

- Concise program -> quite complex and sophisticated synthesizers
- Opacity
- Control



Today's topic: SMT



The Rosette Language

Logical Constraints



Answers!

Answers!

SMT Solvers

OK, what's SMT? Satisfiability Modulo Theories ok, and what's satisfiability??

- SAT: Boolean satisfiability problem; also sometimes called SATISFIABILITY
 - FALSE such that the formula evaluates to TRUE?
 - If yes, the formula is satisfiable
 - unsatisfiable
- Examples:
 - $p \land q$ is satisfiable; (p=TRUE, q=TRUE)
 - $p \land \neg p$ is unsatisfiable
- SAT is NP-complete
 - and using them to solve real problems

Let's back up

• Given a Boolean formula, is there an interpretation of the formula that satisfies it? Can we replace the variables of the Boolean formula with the values TRUE or

• If no assignment out of all possible assignments makes the formula TRUE, it's

...but that hasn't stopped folks from building some seriously efficient SAT solvers

Next few slides shamelessly lifted from...

SAT Solving Basics

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See <u>https://courses.cs.washington.edu/courses/cse507/19au/calendar.html</u> for more



(¬⊅ ∧ ⊤) ∨ **(q** → ⊥)

Atom

truth symbols: \top ("true"), \perp ("false") **propositional variables**: p, q, r, ...

Atom	truth symb	
	propositior	
Literal	an atom α or	

(¬⊅ ∧ ⊤) ∨ (q → ⊥)

- **bols**: \top ("true"), \perp ("false") **nal variables**: p, q, r, ...
- its negation $\neg \alpha$

Atom	truth symbols proposition
Literal	an atom & or
Formula	an atom or the to formulas F_{I} ,
	$\neg F_i$
	$F_1 \wedge F_2$

- $F_1 \lor F_2$ $F_1 \longrightarrow F_2$
- $F_1 \leftrightarrow F_2$

(¬⊅ ∧ ⊤) ∨ (q → ⊥)

pols: \top ("true"), \perp ("false") **nal variables**: p, q, r, ...

its negation $\neg \alpha$

ne application of a **logical connective** 1, F₂:

"not"	(negation)
"and"	(conjunction)
"or"	(disjunction)
"implies"	(implication)
"if and only if"	(iff)

Semantics of propositional logic: interpretations

An **interpretation** *I* for a propositional formula *F* maps every variable in *F* to a truth value:

 $I: \{ p \mapsto true, q \mapsto false, \ldots \}$



Semantics of propositional logic: interpretations

An **interpretation** *I* for a prop *F* maps every variable in *F* to a tru

 $I: \{ p \mapsto \text{true}, q \mapsto \text{false} \}$

I is a **satisfying interpretation** as $I \models F$, if *F* evaluates to true under

I is a **falsifying interpretatio** as $I \nvDash F$, if *F* evaluates to false und

oositional formula uth value:	
e,}	
on of <i>F</i> , written	
on of F, written	
der I.	

Semantics of propositional logic: interpretations

An **interpretation** *I* for a propositional formula *F* maps every variable in *F* to a truth value:

 $I: \{ p \mapsto \text{true}, q \mapsto \text{false}, \ldots \}$

I is a **satisfying interpretation** of *F*, written as $I \models F$, if *F* evaluates to true under *I*.

I is a **falsifying interpretation** of *F*, written as $I \nvDash F$, if *F* evaluates to false under *I*.



Satisfiability & validity of propositional formulas

F is **satisfiable** iff $I \models F$ for some *I*.

F is **valid** iff $I \models F$ for all *I*.



Satisfiability & validity of propositional formulas

F is **satisfiable** iff $I \models F$ for some *I*.

F is **valid** iff $I \models F$ for all *I*.

Duality of satisfiability and validity

F is valid iff $\neg F$ is unsatisfiable.



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Satisfiability & validity of propositional formulas

F is **satisfiable** iff $I \models F$ for some

F is **valid** iff $I \models F$ for all *I*.

Duality of satisfiability and validi

F is valid iff $\neg F$ is unsatisfiable.

e I.	
lity:	If we have a procedure for checking satisfiability, we can also check validity of propositional formulas, and vice versa.

Techniques for deciding satisfiability & validity





Techniques for deciding satisfiability & validity

Search

Enumerate all interpretations (i.e., build a truth table), and check that they satisfy the formula.

Deduction

Assume the formula is invalid, apply proof rules, and check for contradiction in every branch of the proof tree.

SAT solver



Þ	q	þ ^ q	٦q	<i>p</i> ∨ ¬q	F	
0	0	0	I	I	I	Valid.
0	1	0	0	0	1	
	0	0	I	I	I	
		I	0	I		

Proof by search: enumerating interpretations

$$\land q) \rightarrow (p \lor \neg q)$$

Questions?



5 minute breakout chat 5 minute whole-group discussion

10 minute break

Now that we know about SAT...

• Ok so...what's SMT?

• Satisfiability (SAT) Modulo Theories

Next few slides shamelessly lifted from...

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Again, see https://courses.cs.washington.edu/courses/cse507/19au/calendar.html for more









First-Order Logic











Syntax of First-Order Logic (FOL)

Logical symbols

- Connectives: \neg , \land , \lor , \rightarrow , \leftrightarrow
- Parentheses: ()

X Quantifiers: ∀,∃

Non-logical symbols

- Constants: x, y, z
- N-ary functions: f, g
- N-ary predicates: p, q

X Variables: u, v, w

We will only consider the **quantifier-free** fragment of FOL.

In particular, we will consider quantifier-free **ground** formulas.

Semantics of FOL: example

Universe

- A non-empty set of values
- Finite or (un)countably infinite

Interpretation

- Maps a constant symbol c to an element of U: $I[c] \in U$
- Maps an n-ary function symbol f to a function $f_I : U^n \rightarrow U$
- Maps an n-ary predicate symbol p to an n-ary relation $p_I \subseteq U^n$



You decide! Take 1 min.

Satisfiability and validity of FOL

F is **satisfiable** iff $M \models F$ for some structure $M = \langle U, I \rangle$.

F is **valid** iff $M \models F$ for all structure $M = \langle U, I \rangle$.

Duality of satisfiability and validity:

F is valid iff $\neg F$ is unsatisfiable.

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res	
lity:	

Common theories

Equality (and uninterpreted functions)

• x = g(y)

Fixed-width bitvectors

• (b >> I) = c

Linear arithmetic (over R and Z)

•
$$2x + y \leq 5$$

Arrays

• a[i] = x

Theory of equality with uninterpreted functions

Signature: {=, x, y, z, ..., f, g, ..., p, q, ...}

- The binary predicate = is *interpreted*.

Axioms

- $\forall x. x = x$
- $\forall x, y. x = y \rightarrow y = x$
- $\forall x, y, z. x = y \land y = z \rightarrow x = z$

Deciding T=

•

• All constant, function, and predicate symbols are uninterpreted.

• $\forall x_1, \ldots, x_n, y_1, \ldots, y_n$. $(x_1 = y_1 \land \ldots \land x_n = y_n) \rightarrow (f(x_1, \ldots, x_n) = f(y_1, \ldots, y_n))$ • $\forall x_1, \ldots, x_n, y_1, \ldots, y_n$. $(x_1 = y_1 \land \ldots \land x_n = y_n) \rightarrow (p(x_1, \ldots, x_n) \leftrightarrow p(y_1, \ldots, y_n))$

Conjunctions of literals modulo $T_{=}$ is decidable in polynomial time.

```
int abs(int y) {
 return y<0 ? -y : y;
}
int sq(int y) {
 return y*y;
}
int sqabs(int y) {
 return abs(y)*abs(y);
}
```

```
int abs(int y) {
   return y<0 ? -y : y;
}
int sq(int y) {
   return y*y;
}
int sqabs(int y) {
   return abs(y)*abs(y);
}</pre>
```

Are **sq** and **sqabs** equivalent on all 128-bit integers?

```
int abs(int y) {
   return y<0 ? -y : y;
}
int sq(int y) {
   return y*y;
}
int sqabs(int y) {
   return abs(y)*abs(y);
}</pre>
```

Are **sq** and **sqabs** equivalent on all 128-bit integers?

Yes, but the solver takes a while to return an answer because reasoning about multiplication is expensive.

```
int abs(int y) {
   return y<0 ? -y : y;
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}</pre>
```

Are **sq** and **sqabs** equivalent on all 128-bit integers?

Yes, but the solver takes a while to return an answer because reasoning about multiplication is expensive.

What happens if we replace the multiplication with an uninterpreted function?

Theory of fixed-width bitvectors

Signature

- Fixed-width words modeling machine ints, longs, ...
- Arithmetic operations: bvadd, bvsub, bvmul, ...
- Bitwise operations: bvand, bvor, bvnot, ...
- Comparison predicates: bvlt, bvgt, ...
- Equality: =
- Expanded with all constant symbols: x, y, z, ...

Deciding T_{BV}

• NP-complete.

Theories of linear integer and real arithmetic

Signature

- Integers (or reals)
- Predicates: =, \leq .
- Expanded with all constant symbols: x, y, z, ...

Deciding TLIA and TLRA

- NP-complete for linear integer arithmetic (LIA).
- Polynomial time for linear real arithmetic (LRA).
- where c is an integer or real number).

• Arithmetic operations: multiplication by an integer (or real) number, +, -.

• Polynomial time for difference logic (conjunctions of the form $x - y \le c$,

LIA example: compiler optimization



```
int v = a[j];
for (i=1; i<=10; i++) {
    a[j+i] = v;
}</pre>
```

A LIA formula that is unsatisfiable iff this transformation is valid:

LIA example: compiler optimization



```
int v = a[j];
for (i=1; i<=10; i++) {
    a[j+i] = v;
}</pre>
```

A LIA formula that is unsatisfiable iff this transformation is valid:

$$(i \ge 1) \land (i \le 10) \land$$
$$(j + i = j)$$

Theory of arrays

Signature

- Array operations: read, write
- Equality: =
- Expanded with all constant symbols: x, y, z, ...

Axioms

- $\forall a, i, v. read(write(a, i, v), i) = v$
- $\forall a, i, j, v. \neg (i = j) \rightarrow (read(write(a, i, v), j) = read(a, j))$
- $\forall a, b. (\forall i. read(a, i) = read(b, i)) \rightarrow a = b$

Deciding T_A

- Satisfiability problem: NP-complete.
- Used in many software verification tools to model memory.

Basically...

- SAT lets us say simple things
- SMT lets us say...other simple things. But more complicated than SAT!

 - interesting tasks!

And it's enough that we can get to some interesting tasks

On Thursday we'll start playing around with some

Install before Tuesday's class: Z3 SMT solver

We'll use the Python Z3 bindings. First make sure you have Python installed. Then install the Z3 bindings. (https://pypi.org/project/z3-solver/)



Then make sure you can run this program, which I'll also upload in Slack.

from z3 import * x = Int('x')y = Int('y')solve(x > 1, y > 1, x * y + 3 == 7)

To think about for next reading

- them.
- Our silly Python synthesizer from last week wasn't very scale!
- carefully.

 Like last reading, no need to memorize details—mostly want you to know these techniques exist and why we care about

scalable, but there are ways to make enumerative search

 Hierarchical search is the fancy way of saying you can split the problem into multiple subproblems which you can solve separately—this is a key idea for many important synthesis tasks, and you can apply it yourself in many domains. This can improve scalability dramatically. Read the example extra